From theoretical crypto to practice: gloups an abominable gap

Cryptie, Oblazy

Cryptie, O. Blazy (Xlim)

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### 2 Libraries

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### 2 Libraries

3 Funny Cryptography

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Funny Cryptography

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### Definition (Encryption Scheme)

- $\mathcal{E} = (\mathsf{Setup}, \mathsf{EKeyGen}, \mathsf{Encrypt}, \mathsf{Decrypt}):$ 
  - Setup(1<sup>ft</sup>): param;
  - EKeyGen(param): public *encryption* key pk, private *decryption* key dk;
  - Encrypt(pk, m; r): ciphertext c on  $m \in \mathcal{M}$  and pk;
  - Decrypt(dk, c): decrypts c under dk.



Indistinguishability:

Given  $M_0, M_1$ , it should be hard to guess which one is encrypted in C.

Cryptie,	О. B	lazy (X	lim)
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### Definition

An assymetric encryption scheme allows Cryptie, using the public key of Bob, to encrypt a message to Bob in such a way that only Bob, with his secret key, can read it.



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Given q pairs  $(m_i, \sigma_i)$ , it should be hard to output a valid  $\sigma$  on a fresh m.

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### Definition

A signature scheme allows Cryptie, using her secret key, to sign a document in such a way that anybody knowing her public key, for example Bob, can be sure that she signs exactly this document.



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### Definition

A signature scheme allows Cryptie, using her secret key, to sign a document in such a way that anybody knowing her public key, for example Bob, can be sure that she signs exactly this document.





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1 Encryption and Signature: Just a 2 min reminder

### 2 Libraries



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# Libre Crypto libraries? we have a lot of them

NaCL	Public domain
Botan	(simplified) BSD
Boncycastle	MIT License
Cryptlib	Sleepycat License
Crypto++	Boost Software License 1.0 (Public domain for files)
Libgcrypt	LGPLv2.1+
Libtomcrypt	Public License and WTFPL
Nettle	GPLv2+ and LGPLv3+
OpenSSL and LibreSSL	OpenSSL License, original SSLeay Licence
etc	

 $\Rightarrow$  You can even discover some new Free Software license !  $\Rightarrow$  Mostly vanilla crypto...

 $\Rightarrow$  Community knows the good parameter, the good curve but...

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When academics says "this is broken", it is patched (nearly in a timely manner).

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### Example

- First theoretical academic attack on SHA-1 in 2005
- First academic attack that may(?) be used 2010-2015ish.
- Start of the end of SHA-1 2013-2015.
- Summer 2016: Practical attacks.

What about funny crypto?

20+ years later the lucky ones are just starting to be used (in weird Blockchains).



- Weird signatures
- Strange encryption
- Crazy stuff

 $\Rightarrow$  Let's talk about funny crypto

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### 2 Libraries

Sunny Cryptography

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## Weird signatures



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### Definition

A sanitizable signature allows Alice to signs a text in such a way that she can give Cryptie the right to modify some parts of it while keeping a correct signature of her on this modified message.



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[CvH91]

### Definition

A group signature allows Bob to signs as a member of a group in such a way that only a special (optional) entity, an "Opener", would be able to know that HE was the signer of the given message.



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[CvH91]

### Definition

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# Group Signatures

[CvH91]

### Definition

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# Group Signatures

[CvH91]

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### Definition

A group *ring* signature allows Bob to signs as a member of a group, *that he built alone*, in such a way that <del>only a special (optional) entity, an "Opener", *no one* would be able to know that HE was the signer of the given message.</del>



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[RST01]

### Definition

A group *ring* signature allows Bob to signs as a member of a group, *that he built alone*, in such a way that only a special (optional) entity, an "Opener", *no one* would be able to know that HE was the signer of the given message.



The only technology using it is some Blockchain implementation...

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### Definition

A blind signature allows Alice to signs a letter "through" its envelope. If later, she sees two documents she signs, she won't be able to know which text she signs when.



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### Definition

A blind signature allows Alice to signs a letter "through" its envelope. If later, she sees two documents she signs, she won't be able to know which text she signs when.



Cryptie, O. Blazy (Xlim)	)
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## Strange encryption



Cryptie, O. Blazy (Xlim)

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### Definition

In an Homomorphic Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using a secret decryption key. Ciphertexts can be combined, so that the decryption leads to the combination of the plaintext



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### Definition

In a Threshold Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using **at least k** secret decryption keys.





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### Definition

In a Threshold Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using **at least k** secret decryption keys.





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### Definition

In a Threshold Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using **at least k** secret decryption keys.



### Definition

In a Threshold Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using **at least k** secret decryption keys.



A (1) < (1) < (1) < (1) </p>
[FN94]

#### Definition

In a Broadcast Encryption, a user encrypts a message M for a subset of users. The resulting ciphertext can then be decrypted using one of k secret decryption key.





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[Sha01]

#### Definition

In an Identity-based Encryption, a user encrypts a message M, using a public encryption key user identity. The resulting ciphertext can then be decrypted using a secret decryption key.



# [SW04]

#### Definition

In an Attribute-based Encryption, a user encrypts a message M, using a public encryption key corresponding to some policy. The resulting ciphertext can then be decrypted using a secret decryption key credential fitting the policy.



[GGSW13]

#### Definition

In a Witness Encryption, a user encrypts a message M, using a public encryption key. The resulting ciphertext can then be decrypted using a secret decryption key witness of some property.



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### Zero-Knowledge Proof





Interactive method for Alice to prove to Bob that she knows something  $\mathcal{S}$  without revealing anything other than this fact.

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#### Definition

Functions that can be evaluated in two different ways, either with a *secret* hashing key hk or with a *public* projected key hp and a secret witness



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Any encryption of a solution of a NP problem :

- encryption of a password
- encryption of a credential
- solution of an equation
- etc.

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### Conditional Action



 $\rightsquigarrow$  An honest user learns the output.  $\rightsquigarrow$  The server learns nothing.

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 $\rightsquigarrow$  An honest user learns the output iff he possesses the signature.  $\rightsquigarrow$  The server learns nothing.

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[LDB05]



 $\rightsquigarrow$  The User learns the value of line but nothing else.  $\rightsquigarrow$  The Database learns nothing.

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## Authenticated Key Exchange



→ The Users have the same shared key at the end, if they have the same password → Otherwise they learn nothing

 $\leadsto$  Can be done with other things than password

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[BM92]

## Authenticated Key Exchange



 $\rightsquigarrow$  The Users have the same shared key at the end, if they have the same password  $\rightsquigarrow$  Otherwise they learn nothing  $\rightsquigarrow$  Can be done with other things than password

[BM92]

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### Thank you

If you are interested in any of these, contact us. Cryptie: me@cryptie.eu or cryptie@fsfe.org O.Blazy: olivier.blazy@unilim.fr

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#### Thank you

If you are interested in any of these, contact us. Cryptie: me@cryptie.eu or cryptie@fsfe.org O.Blazy: olivier.blazy@unilim.fr PS: Looking for a PhD student

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### Sources

Thanks to :



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