

RUHR-UNIVERSITÄT BOCHUM Round-optimal Signature, developing new tools to improve efficiency . 2013

O. Blazy Horst Görtz Institute for IT Security / Ruhr-University Bochumort Cortz Institut







#### Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

### 1 General Remarks

### 2 Building blocks



Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013



- 2 Building blocks
- 3 Non-Interactive Proofs of Knowledge







- 2 Building blocks
- 3 Non-Interactive Proofs of Knowledge
- 4 Interactive Implicit Proofs



#### Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

RUB

## Proof of Knowledge





<u> </u>	<	
	· · · · · · · · · · · · · · · · · · ·	
	·	
- <b>m</b> -		

Alice

Bob

- $_{\S}$  interactive method for one party to prove to another the knowledge of a secret  $\mathcal{S}.$
- 1. Completeness:  ${\mathcal S}$  is true  $\rightsquigarrow$  verifier will be convinced of this fact
- 2. Soundness:  ${\cal S}$  is false  $\rightsquigarrow$  no cheating prover can convince the verifier that  ${\cal S}$  is true

Classical Instantiations : Schnorr proofs, Sigma Protocols ... Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013 RUHR-UNIVERSITÄT BOCHUM

## Zero-Knowledge Proof Systems





## § Introduced in 1985 by Goldwasser, Micali and Rackoff.

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

## Zero-Knowledge Proof Systems





 $_{\S}$  Introduced in 1985 by Goldwasser, Micali and Rackoff.

 $\rightsquigarrow$  Reveal nothing other than the validity of assertion being proven

# Zero-Knowledge Proof Systems



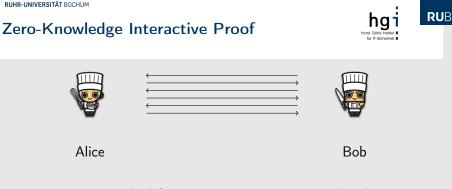


§ Introduced in 1985 by Goldwasser, Micali and Rackoff.

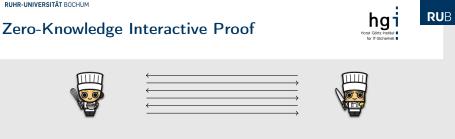
 $\rightsquigarrow$  Reveal nothing other than the validity of assertion being proven

- § Used in many cryptographic protocols
  - Anonymous credentials
  - Anonymous signatures
  - Online voting

o ...



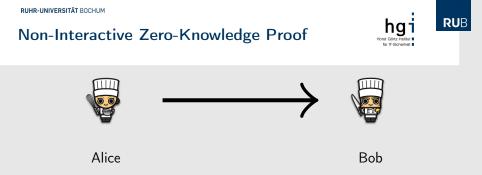
§ interactive method for one party to prove to another that a statement S is true, without revealing anything other than the veracity of S.



Alice

Bob

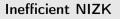
- § interactive method for one party to prove to another that a statement S is true, without revealing anything other than the veracity of S.
- 1. Completeness: if S is true, the honest verifier will be convinced of this fact
- 2. Soundness: if S is false, no cheating prover can convince the honest verifier that it is true
- Round-Optimal Signature Horst Cort in Stitute for M-security heating verifier learns anything 48



- $_{\$}$  non-interactive method for one party to prove to another that a statement  ${\cal S}$  is true, without revealing anything other than the veracity of  ${\cal S}.$
- 1. Completeness:  ${\mathcal S}$  is true  $\rightsquigarrow$  verifier will be convinced of this fact
- 2. Soundness: S is false  $\rightsquigarrow$  no cheating prover can convince the verifier that S is true
- 3. Zero-knowledge: S is true  $\sim$  no cheating verifier learns anything Round-Optimal Signature that this fact Institute for IT-Security | 2013 6/48

# History of NIZK Proofs





§ Blum-Feldman-Micali, 1988.

§ ...

§ De Santis-Di Crescenzo-Persiano, 2002.

# History of NIZK Proofs



## Inefficient NIZK

- § Blum-Feldman-Micali, 1988.
- § ...
- § De Santis-Di Crescenzo-Persiano, 2002.

Alternative: Fiat-Shamir heuristic, 1986: interactive ZK proof  $\rightsquigarrow$  NIZK But limited by the Random Oracle

# History of NIZK Proofs



## Inefficient NIZK

- § Blum-Feldman-Micali, 1988.
- § ...
- § De Santis-Di Crescenzo-Persiano, 2002.

**Alternative:** Fiat-Shamir heuristic, 1986: interactive ZK proof → NIZK But limited by the Random Oracle

## Efficient NIZK

- § Groth-Ostrovsky-Sahai, 2006.
- § Groth-Sahai, 2008.

RUHR-UNIVERSITÄT BOCHUM

## Applications of NIZK Proofs





- § Fancy signature schemes
  - group signatures
  - ring signatures
  - traceable signatures
- § Efficient non-interactive proof of correctness of shuffle
- § Non-interactive anonymous credentials
- § CCA-2-secure encryption schemes (with public verifiability)
- § Identification
- § E-voting, E-cash

§ ...



## Soundness

§ Only people proving they know the expected secret should be able to access the information.

## Zero-Knowledge

§ The authority should not learn said secret.





### 2 Building blocks

- Bilinear groups aka Pairing-friendly environments
- Commitment / Encryption
- Signatures
- Security hypotheses

### 3 Non-Interactive Proofs of Knowledge

4 Interactive Implicit Proofs

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

## Symmetric bilinear structure



 $(p, \mathbb{G}, \mathbb{G}_T, e, g)$  bilinear structure:

§ G, G<sub>T</sub> multiplicative groups of order p  $\circ p = prime integer$ 

$$\begin{array}{l} \{ \langle g \rangle = \mathbb{G} \\ \{ e : \mathbb{G} \times \mathbb{G} \to \mathbb{G}_{\mathcal{T}} \\ \circ \langle e(g,g) \rangle = \mathbb{G}_{\mathcal{T}} \\ \circ e(g^a,g^b) = e(g,g)^{ab}, \ a, b \in \mathbb{Z} \end{array}$$

deciding group membership, group operations, } efficiently computable. ξ bilinear map

## Definition 1 (Encryption Scheme)

- $\mathcal{E} = (\mathsf{Setup}, \mathsf{EKeyGen}, \mathsf{Encrypt}, \mathsf{Decrypt})$ :
  - § Setup $(1^{\Re})$ : param;
  - § EKeyGen(param): public encryption key pk, private decryption key dk;
  - § Encrypt(pk, m; r): ciphertext c on  $m \in \mathcal{M}$  and pk;
  - § Decrypt(dk, c): decrypts c under dk.



Indistinguishability: Given  $M_0, M_1$ , it should be hard to guess which one is encrypted in C.

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

### Definition 2 (Linear Encryption)

- § Setup(1<sup> $\Re$ </sup>): Generates a multiplicative group (p,  $\mathbb{G}$ , g).
- § EKeyGen<sub> $\mathcal{E}$ </sub>(param): dk =  $(\mu, \nu) \stackrel{\{\sc smallmatrix}}{\leftarrow} \mathbb{Z}_p^2$ , and pk =  $(X_1 = g^{\mu}, X_2 = g^{\nu})$ .
- § Encrypt( $pk = (X_1, X_2), M; \alpha, \beta$ ): For M, and random  $\alpha, \beta \leftarrow \mathbb{Z}_p^2$ ,  $\mathcal{C} = (c_1 = X_1^{\alpha}, c_2 = X_2^{\beta}, c_3 = g^{\alpha+\beta} \cdot M).$
- § Decrypt(dk =  $(\mu, \nu), C = (c_1, c_2, c_3)$ ): Computes  $M = c_3/(c_1^{1/\mu}c_2^{1/\nu})$ .

### Randomization

$$\mathsf{Random}(\mathsf{pk}, \mathcal{C}; r, s) : \mathcal{C}' = (c_1 X_1^r, c_2 X_2^s, c_3 g^{r+s}) = (X_1^{\alpha+r}, X_2^{\beta+s}, g^{\alpha+r+\beta+s} \cdot M)$$

RUR

(BBS04

#### RUHR-UNIVERSITÄT BOCHUM





# Definition 3 (Signature Scheme)

- $\mathcal{S} = (\mathsf{Setup}, \mathsf{SKeyGen}, \mathsf{Sign}, \mathsf{Verif}):$ 
  - § Setup $(1^{\mathfrak{K}})$ : param;
  - § SKeyGen(param): public verification key vk, private signing key sk;
  - § Sign(sk, m; s): signature  $\sigma$  on m, under sk;
  - § Verif(vk,  $m, \sigma$ ): checks whether  $\sigma$  is valid on m.

Unforgeability: Given q pairs  $(m_i, \sigma_i)$ , it should be hard to output a valid  $\sigma$  on a fresh m.

### Definition 4 (Waters Signature)

- § Setup<sub>S</sub>(1<sup> $\Re$ </sup>): Generates (p,  $\mathbb{G}_T$ , e, g), an extra h, and ( $u_i$ ) for the Waters function ( $\mathcal{F}(m) = u_0 \prod_i u_i^{m_i}$ ).
- § SKeyGen<sub>S</sub>(param): Picks  $x \stackrel{\$}{\leftarrow} \mathbb{Z}_p$  and outputs  $\mathsf{sk} = h^x$ , and  $\mathsf{vk} = g^x$ ;
- § Sign(sk, m; s): Outputs  $\sigma(m) = (sk\mathcal{F}(m)^s, g^s);$
- § Verif(vk, m,  $\sigma$ ): Checks the validity of  $\sigma$ :  $e(g, \sigma_1) \stackrel{?}{=} e(\mathcal{F}(m), \sigma_2) \cdot e(vk, h)$

### Randomization

$$\mathsf{Random}(\sigma; r) : \sigma' = \left(\sigma_1 \mathcal{F}(m)^r, \sigma_2 g^r\right) = \left(\mathsf{sk} \mathcal{F}(m)^{r+s}, g^{r+s}\right)$$

RUB

(Wat05)



# Definition 5 (DL)

Given  $g, h \in \mathbb{G}^2$ , it is hard to compute  $\alpha$  such that  $h = g^{\alpha}$ .

# Definition 6 (CDH)

Given  $g, g^a, h \in \mathbb{G}^3$ , it is hard to compute  $h^a$ .

## Definition 7 (DLin)

Given  $u, v, w, u^a, v^b, w^c \in \mathbb{G}^6$ , it is hard to decide whether c = a + b.





### 1 General Remarks

## 2 Building blocks

## 3 Non-Interactive Proofs of Knowledge

- Groth Sahai methodology
- Motivation
- Signature on Ciphertexts
- Application to other protocols
- Waters Programmability

### 4 Interactive Implicit Proofs

## Groth-Sahai Proof System



§ Pairing product equation (PPE): for variables  $\mathcal{X}_1, \ldots, \mathcal{X}_n \in \mathbb{G}$ 

$$(E):\prod_{i=1}^{n}e(A_{i},\mathcal{X}_{i})\prod_{i=1}^{n}\prod_{j=1}^{n}e(\mathcal{X}_{i},\mathcal{X}_{j})^{\gamma_{i,j}}=t_{T}$$

determined by  $A_i \in \mathbb{G}$ ,  $\gamma_{i,j} \in \mathbb{Z}_p$  and  $t_T \in \mathbb{G}_T$ .

 $_{\$}\,$  Groth-Sahai  $\rightsquigarrow$  WI proofs that elements in  $\mathbb G$  that were committed to satisfy PPE

## Groth-Sahai Proof System



§ Pairing product equation (PPE): for variables  $\mathcal{X}_1, \ldots, \mathcal{X}_n \in \mathbb{G}$ 

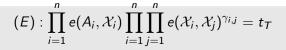
$$(E):\prod_{i=1}^{n}e(A_{i},\mathcal{X}_{i})\prod_{i=1}^{n}\prod_{j=1}^{n}e(\mathcal{X}_{i},\mathcal{X}_{j})^{\gamma_{i,j}}=t_{T}$$

determined by  $A_i \in \mathbb{G}$ ,  $\gamma_{i,j} \in \mathbb{Z}_p$  and  $t_T \in \mathbb{G}_T$ .

 $_{\$}\,$  Groth-Sahai  $\rightsquigarrow$  WI proofs that elements in  $\mathbb G$  that were committed to satisfy PPE

Setup(G): commitment key ck; Com(ck,  $X \in G$ ;  $\rho$ ): commitment  $\vec{c_X}$  to X; Prove(ck,  $(X_i, \rho_i)_{i=1,...,n}$ , (E)): proof  $\phi$ ; Verify(ck,  $\vec{c_{X_i}}$ , (E),  $\phi$ ): checks whether  $\phi$  is valid.







$$(E):\prod_{i=1}^{n}e(A_{i},\mathcal{X}_{i})\prod_{i=1}^{n}\prod_{j=1}^{n}e(\mathcal{X}_{i},\mathcal{X}_{j})^{\gamma_{i,j}}=t_{T}$$

### **Properties:**

- § correctness
- § soundness
- § witness-indistinguishability



$$(E):\prod_{i=1}^{n}e(A_{i},\mathcal{X}_{i})\prod_{i=1}^{n}\prod_{j=1}^{n}e(\mathcal{X}_{i},\mathcal{X}_{j})^{\gamma_{i,j}}=t_{T}$$

### **Properties:**

- § correctness
- § soundness
- § witness-indistinguishability
- § randomizability Commitments and proofs are publicly randomizable.

## **Electronic Voting**



For dessert, we let people vote

- $\checkmark$  Chocolate Cake
- $\checkmark\,$  Cheese Cake
- ✓ Fruit Salad
- $\checkmark$  Brussels Sprout

After collection, we count the number of ballots:

Chocolate Cake	123
Cheese Cake	79
Fruit Salad	42
Brussels sprout	1



## Authentication

- $\S$  Only people authorized to vote should be able to vote
- $\S$  People should be able to vote only once

## Anonymity

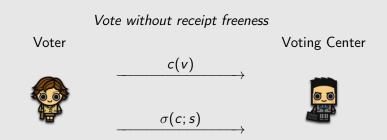
- $\S$  Votes and voters should be anonymous
- $\triangle$  Receipt freeness



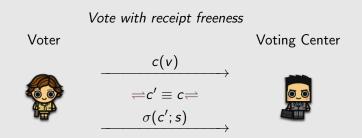
## Homomorphic Encryption and Signature approach

- § The voter generates his vote v.
- § The voter encrypts v to the server as c.
- § The voter signs c and outputs  $\sigma$ .
- $(c, \sigma)$  is a ballot unique per voter, and anonymous.
- § Counting: granted homomorphic encryption  $C = \prod c$ .
- § The server decrypts C.



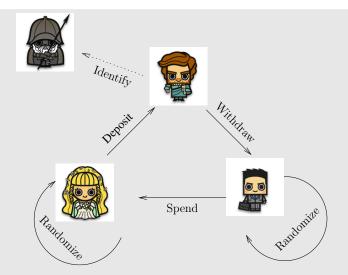






## **Electronic Cash**





#### Protocol

- $\S$  Withdrawal: A user get a coin c from the bank
- $\S$  Spending: A user pays a shop with the coin c
- $\S$  Deposit: The shop gives the coin c back to the bank

## **Electronic Coins**

Expected properties

- $\checkmark$  Unforgeability  $\rightsquigarrow$  Coins are signed by the bank
- $\checkmark$  No Double-Spending  $\rightsquigarrow$  Each coin is unique
- ✓ Anonymity → Blind Signature

#### Definition 8 (Blind Signature)

A blind signature allows a user to get a message m signed by an authority into  $\sigma$  so that the authority *even powerful* cannot recognize later the pair  $(m, \sigma)$ .

Chaum 81



Fischlin 06

# Round-Optimal Blind Signature

- § The user encrypts his message m in c.
- § The signer then signs c in  $\sigma$ .
- § The user verifies  $\sigma$ .
- § He then encrypts  $\sigma$  and c into  $C_{\sigma}$  and C and generates a proof  $\pi$ .
- §  $\pi$ :  $C_{\sigma}$  is an encryption of a signature over the ciphertext *c* encrypted in C, and this *c* is indeed an encryption of *m*.
- § Anyone can then use  $C, C_{\sigma}, \pi$  to check the validity of the signature.



§ A user should be able to encrypt a ballot.

RUB

- § He should be able to sign this encryption.
- § Receiving this vote, one should be able to randomize for *Receipt-Freeness*.

# E-Cash

- $\S~$  A user should be able to encrypt a token
- $\S$  The bank should be able to sign it providing Unforgeability
- § This signature should now be able to be randomized to provide *Anonymity*

# Our Solution

- $\S$  Same underlying requirements;
- § Advance security notions in both schemes requires to extract some kind of signature on the associated plaintext;
   d-Optimal Signature | Horst Görtz Institute for IT-Security | 2013 27/48

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013 8 General Framework for Signature on Randomizable Ciphertexts:

## **Commutative properties**



#### RUB

#### Encrypt

To encrypt a message *m*:

$$c = (\mathsf{pk}_1^{r_1}, \mathsf{pk}_2^{r_2}, \mathcal{F}(m) \cdot g^{r_1+r_2})$$

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

### **Commutative properties**



## Encrypt

To encrypt a message *m*:

$$c = (\mathsf{pk}_1^{r_1}, \mathsf{pk}_2^{r_2}, \mathcal{F}(m) \cdot g^{r_1+r_2})$$

#### Sign $\circ$ Encrypt

To sign a valid ciphertext  $c_1, c_2, c_3$ , one has simply to produce.

$$\sigma = (c_1^{s}, c_2^{s}, \mathsf{sk} \cdot c_3^{s}, \mathsf{pk}_1^{s}, \mathsf{pk}_2^{s}, g^{s}) .$$

## Commutative properties



RUB

#### Encrypt

To encrypt a message *m*:

$$c = (\mathsf{pk}_1^{r_1}, \mathsf{pk}_2^{r_2}, \mathcal{F}(m) \cdot g^{r_1+r_2})$$

#### Sign $\circ$ Encrypt

To sign a valid ciphertext  $c_1, c_2, c_3$ , one has simply to produce.

$$\sigma = (c_1^{s}, c_2^{s}, \mathsf{sk} \cdot c_3^{s}, \mathsf{pk}_1^{s}, \mathsf{pk}_2^{s}, g^{s}) .$$

## $\mathsf{Decrypt}\,\circ\,\mathsf{Sign}\,\circ\,\mathsf{Encrypt}$

Rouse Rouse Signature | Horst Görtz Institute for IT-Security | 2013

#### Definition 9 (Signature on Ciphertexts)

- $\mathcal{SE} = (\mathsf{Setup}, \mathsf{SKeyGen}, \mathsf{EKeyGen}, \mathsf{Encrypt}, \mathsf{Sign}, \mathsf{Decrypt}, \mathsf{Verif}):$ 
  - § Setup $(1^{\mathfrak{K}})$ : param<sub>e</sub>, param<sub>s</sub>;
  - § EKeyGen(param<sub>e</sub>): pk, dk;
  - § SKeyGen(param<sub>s</sub>): vk, sk;
  - § Encrypt(pk, vk, m; r): produces c on  $m \in M$  and pk;
  - § Sign(sk, pk, c; s): produces  $\sigma$ , on the input c under sk;
  - § Decrypt(dk, vk, c): decrypts c under dk;
  - § Verif(vk, pk,  $c, \sigma$ ): checks whether  $\sigma$  is valid.

# Definition 10 (Extractable Randomizable Signature on Ciphertexts)

SE=(Setup, SKeyGen, EKeyGen, Encrypt, Sign, Random, Decrypt, Verif, SigE

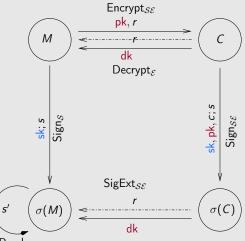
 $\mbox{\sc 8}$  Random(vk, pk, c,  $\sigma; r', s')$  produces c' and  $\sigma'$  on c', using addi-

tional coins; Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

 $\circ$  C:=  $\Gamma_{i}$  + (all i -)  $\bullet_{i}$  +  $\bullet_{i}$  =  $\bullet_{i}$  =  $\bullet_{i}$  =  $\bullet_{i}$  =  $\bullet_{i}$ 

JB

# Randomizable Signature on Ciphertexts [PKC 2011: BFPV]



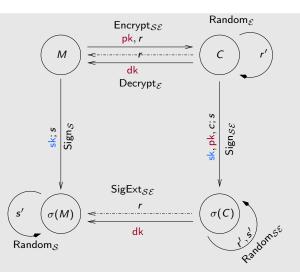
Random<sub>S</sub>

RUB

### Extractable SRC



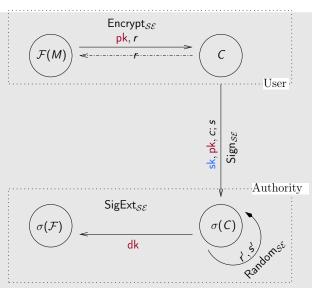




**E-Voting** 

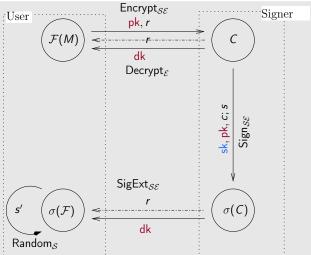






Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

**Blind Signature** 



[PKC 2011: BFPV]

······

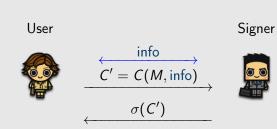
hgi

für IT-Sicherheit

RUB

## Partially-Blind Signature



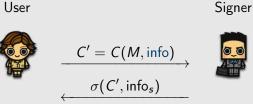


Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

## Partially-Blind Signature

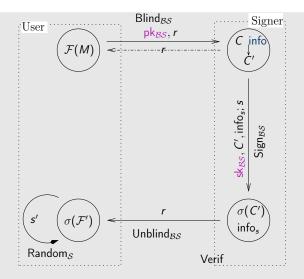






Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

# Signer-Friendly Partially Blind Signature [SCN 2012: BPV]



Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

RUB

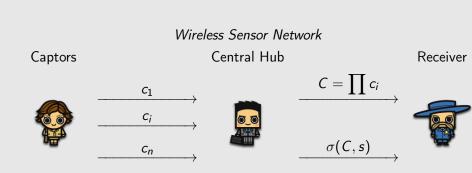
Horst Görtz Institut

RUHR-UNIVERSITÄT BOCHUM

## **Multi-Source Blind Signatures**



RUB



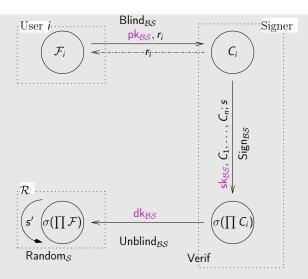
## Multi-Source Blind Signatures **BPV**]

## [SCN 2012:

Horst Görtz Institut für IT-Sicherheit











#### RUB

#### **Different Generators**

§ Each captor has a disjoint set of generators for the Waters function





#### **Different Generators**

- § Each captor has a disjoint set of generators for the Waters function
- § Enormous public key





#### **Different Generators**

- § Each captor has a disjoint set of generators for the Waters function
- § Enormous public key

#### A single set of generators

 $\S~$  The captors share the same set of generators





#### **Different Generators**

- § Each captor has a disjoint set of generators for the Waters function
- § Enormous public key

#### A single set of generators

- § The captors share the same set of generators
- § Waters over a non-binary alphabet?

# Programmability of Waters over a non-binary alphabet





# Definition 11 ((m, n)-programmability)

*F* is (m, n) programmable if given g, h there is an efficient trapdoor producing  $a_X, b_X$  such that  $F(X) = g^{a_X} h^{b_X}$ , and for all  $X_i, Z_j, Pr[a_{X_1} = \dots = a_{X_m} = 0 \land a_{Z_1} \cdot \dots \cdot a_{Z_n} \neq 0]$  is not negligible.

## (1, q)-Programmability of Waters function

Why do we need it: Unforgeabilty, q signing queries, 1 signature to exploit.

 $\sim$  Choose independent and uniform elements  $(a_i)_{(1,...,\ell)}$  in  $\{-1,0,1\}$ , and random exponents  $(b_i)_{(0,...,\ell)}$ , and setting  $a_0 = -1$ . Then  $u_i = g^{a_i} h^{b_i}$ .

$$\mathcal{F}(m) = u_0 \prod u_i^{m_i} = g^{\sum_{\delta_i} a_i} h^{\sum_{\delta_i} b_i} = g^{a_m} h^{b_m}$$

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013



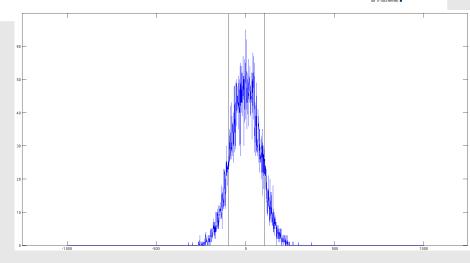
# Non (2, 1)-programmability

Waters over a non-binary alphabet is not (2, 1)-programmable.

# (1, q)-programmability

Waters over a polynomial alphabet remains (1, q)-programmable.

# Sum of random walks on polynomial alphabets



#### Local Central Limit Theorem ⇒ Lindeberg Feller

Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013

RUB

na

- § New primitive: Signature on Randomizable Ciphertexts [PKC 2011: BFPV]
- ✓ One Round Blind Signature
- ✓ Receipt Free E-Voting
- ✓ Signer-Friendly Blind Signature
- ✓ Multi-Source Blind Signature

# Efficiency

- § DLin + CDH :  $9\ell$  + 24 Group elements.
- S SXDH + CDH<sup>+</sup> :  $6\ell$  + 15,  $6\ell$  + 7 Group elements.

RUB

[PKC 2011: BFPV] [PKC 2011: BFPV]

[SCN 2012: BPV] [SCN 2012: BPV]





#### 1 General Remarks

## 2 Building blocks

#### 3 Non-Interactive Proofs of Knowledge

#### 4 Interactive Implicit Proofs

- Motivation
- Smooth Projective Hash Function
- Application to previous protocols

# **Smooth Projective Hash Functions**

## Definition



[CS02]

Let  $\{H\}$  be a family of functions:

- $\S$  X, domain of these functions
- § L, subset (a language) of this domain

such that, for any point x in L, H(x) can be computed by using

- § either a secret hashing key hk:  $H(x) = \text{Hash}_{L}(hk; x);$
- § or a *public* projected key hp:  $H'(x) = \text{ProjHash}_L(\text{hp}; x, w)$

Public mapping  $hk \mapsto hp = ProjKG_L(hk, x)$ 



For any  $x \in X$ ,  $H(x) = \text{Hash}_L(hk; x)$ For any  $x \in L$ ,  $H(x) = \text{ProjHash}_L(hp; x, w)$ w witness that  $x \in L$ ,  $hp = \text{ProjKG}_L(hk, x)$ 



RUB

For any  $x \in X$ ,  $H(x) = \text{Hash}_L(hk; x)$ For any  $x \in L$ ,  $H(x) = \text{ProjHash}_L(hp; x, w)$ w witness that  $x \in L$ ,  $hp = \text{ProjKG}_L(hk, x)$ 

#### Smoothness

For any  $x \notin L$ , H(x) and hp are independent



RUE

For any  $x \in X$ ,  $H(x) = \text{Hash}_L(hk; x)$ For any  $x \in L$ ,  $H(x) = \text{ProjHash}_L(hp; x, w)$ w witness that  $x \in L$ ,  $hp = \text{ProjKG}_L(hk, x)$ 

#### Smoothness

For any  $x \notin L$ , H(x) and hp are independent

#### Pseudo-Randomness

For any  $x \in L$ , H(x) is pseudo-random, without a witness w



RUE

For any  $x \in X$ ,  $H(x) = \text{Hash}_L(hk; x)$ For any  $x \in L$ ,  $H(x) = \text{ProjHash}_L(hp; x, w)$ w witness that  $x \in L$ ,  $hp = \text{ProjKG}_L(hk, x)$ 

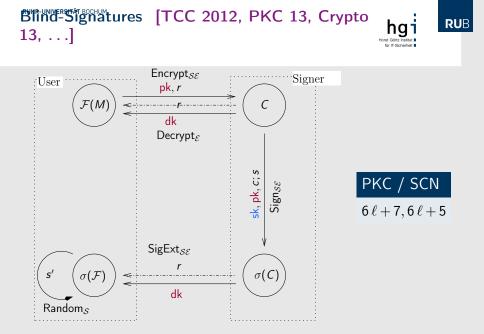
#### Smoothness

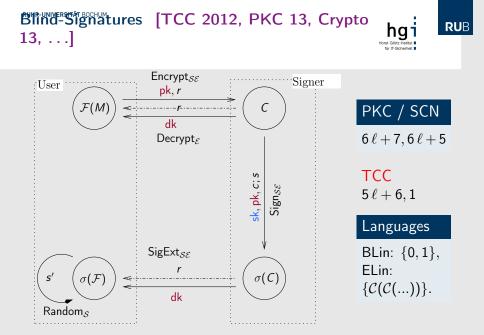
For any  $x \notin L$ , H(x) and hp are independent

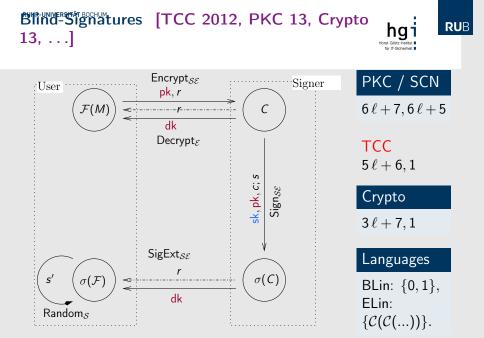
#### Pseudo-Randomness

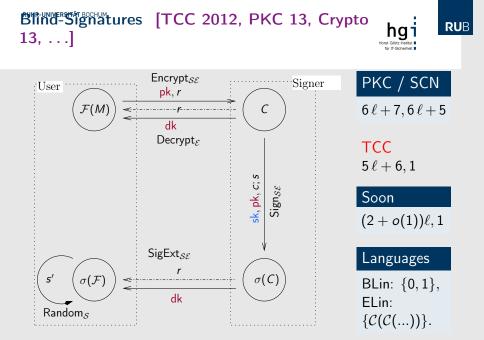
For any  $x \in L$ , H(x) is pseudo-random, without a witness w

The latter property requires L to be a hard-partitioned subset of X.











## Groth-Sahai

- § Allows to combine efficiently classical building blocks
- § Allows several kind of new signatures under standard hypotheses

#### Smooth Projective Hash Functions

- § Can handle more general languages under better hypotheses
- § Do not add any extra-rounds in an interactive scenario
- $\S$  More efficient in the usual cases

#### Groth-Sahai

- § Allows to combine efficiently classical building blocks
- § Allows several kind of new signatures under standard hypotheses

## Smooth Projective Hash Functions

- § Can handle more general languages under better hypotheses
- § Do not add any extra-rounds in an interactive scenario
- $\S$  More efficient in the usual cases



RUB



RUHR-UNIVERSITÄT BOCHUM Many thanks for your attention!

Any questions?

More details are available in the full version...



Round-Optimal Signature | Horst Görtz Institute for IT-Security | 2013